

4.4

(a) PRIMARY $x^2 + y^2 = s$

$$(20-y)^2 + y^2 = s$$

$$400 - 40y + y^2 + y^2 = s$$

$$400 - 40y + 2y^2 = s$$

$$0 = -40 + 4y = s'$$

$$\frac{40}{4} = \frac{4y}{4}$$

$$10 = y$$

SECONDARY $x+y=20 \leftarrow$
 $\boxed{x=20-y}$

FDT	DECR.	INCR
-	"	"
10		

$10 \leq y \leq 10$ min.

$0 \leq x \leq 20$ max.

(b) $x + \sqrt{y} = s$

$$20-y + y^{1/2} = s$$

$$0 = -y + y^{-1/2} = s'$$

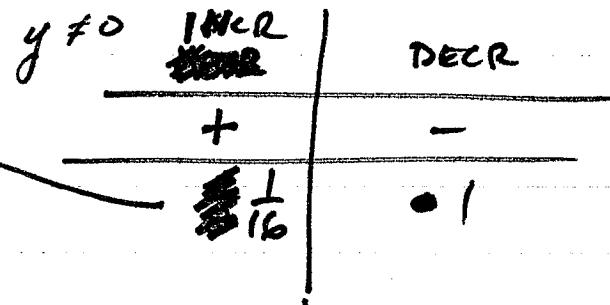
$$1 = \frac{1}{2}y^{-1/2}$$

$$1 = \frac{1}{2\sqrt{y}}$$

$$2\sqrt{y} = 1$$

$$\sqrt{y} = \frac{1}{2}$$

$$y = (\frac{1}{2})^2 = \frac{1}{4}$$



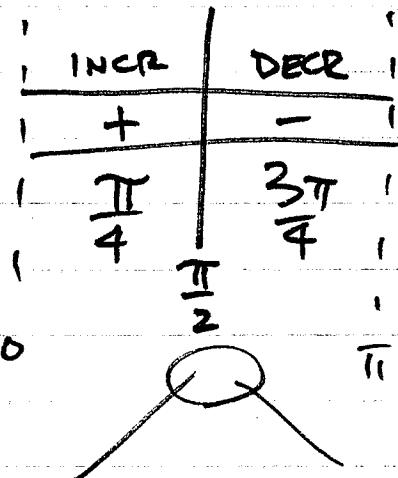
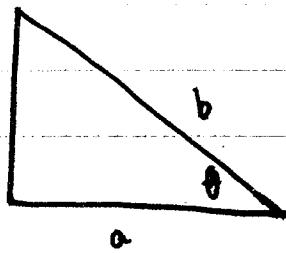
$\frac{1}{4} \leq y \leq 19\frac{3}{4}$ max

$0 \leq x \leq 20$ min

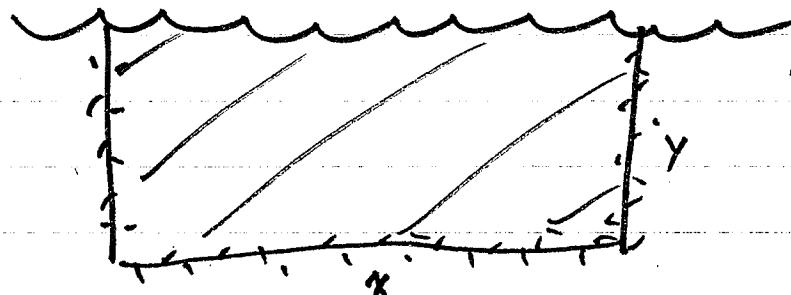
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$$15) A = \frac{1}{2} ab \sin \theta$$

$$A' = \frac{1}{2} ab \cos \theta = 0$$



9)



PRIMARY : $A = xy$
 $A = (800 - 2y)y$

$$A = 800y - 2y^2$$

$$A' = 800 - 4y = 0$$

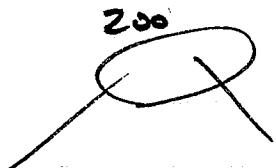
$$800 = 4y$$

$$200 = y$$

SECONDARY : $P = x + 2y = 800$
 $x = 800 - 2y$

FDT

INCR	DECR
+	-
100	300



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(6)



$$\text{primary: } SA = \pi r^2 + 2\pi r h$$

$$= \pi r^2 + 2\pi r \left(\frac{1000}{\pi r^2} \right)$$

$$SA = \pi r^2 + 2000r^{-1}$$

$$(SA)' = 2\pi r - 2000r^{-2} = 0 \quad r \neq 0$$

$$\text{secondary: } V = \pi r^2 h$$

$$\frac{1000}{\pi r^2} = \frac{\pi r^2 h}{\pi r^2}$$

$$2\pi r = \frac{2000}{r^2}$$

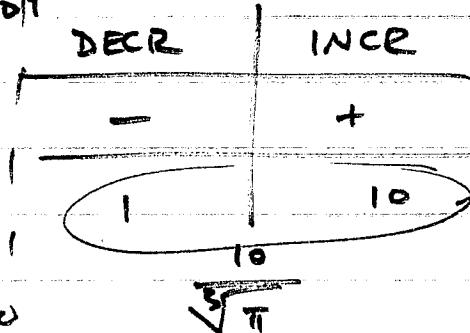
$$2\pi r^3 = 2000$$

$$\pi r^3 = 1000$$

$$r^3 = \frac{1000}{\pi}$$

$$r = \sqrt[3]{\frac{1000}{\pi}}$$

FDT



BECAUSE THE FUNCTION CHANGES FROM DECREASING TO INCREASING,
THERE IS A MINIMUM AT $x = \sqrt[3]{\frac{1000}{\pi}}$.

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1) x - nonnegative number

y - another nonnegative number

$$x+y=20 \quad \text{secondary}$$

$$y = \boxed{20-x}$$

$$(a) S = x^2 + y^2 \quad \text{primary}$$

$$S = x^2 + (20-x)^2$$

$$S = x^2 + 400 - 40x + x^2$$

$$S = 400 - 40x + 2x^2$$

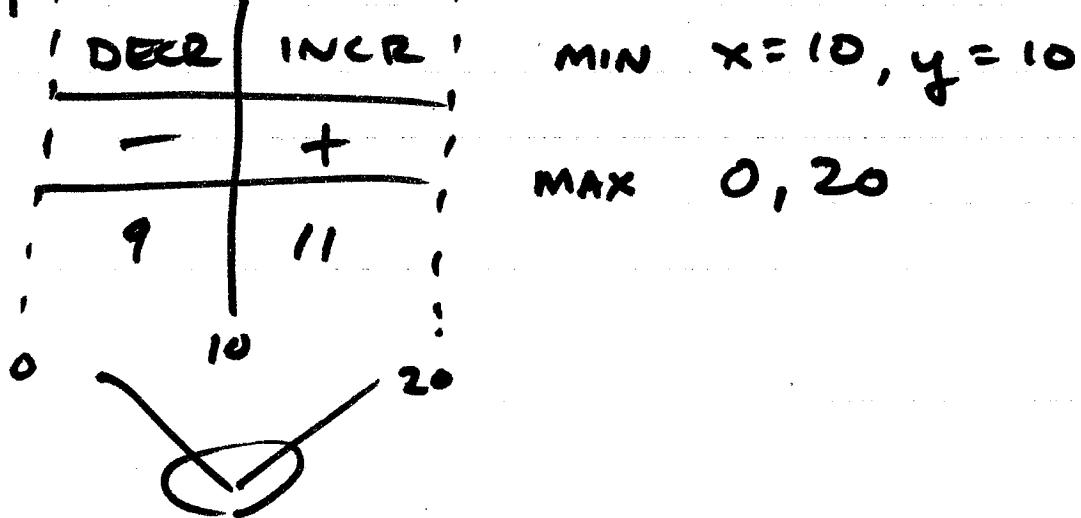
$$S' = -40 + 4x = 0$$

$$4x = 40$$

$$x = 10$$

FDT'

DECR	INCR	MIN $x=10, y=10$
-	+	
9	11	
0	10	MAX 0, 20



#1 4.4

(6) $x + \sqrt{y} = 5$ primary $x + y = 20$ secondary

$$x + y^{1/2} = 5$$

$$x = 20 - y$$

$$20 - y + y^{1/2} = 5$$

y is undefined \Rightarrow

$$-1 + \frac{1}{2}y^{-1/2} = 5' = 0$$

$$\boxed{y \neq 0}$$

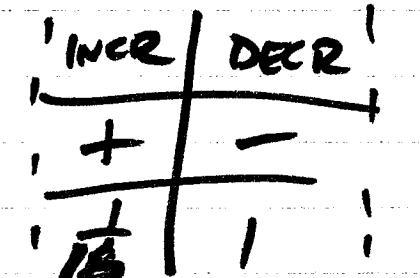
$$\frac{1}{2}y^{-1/2} = 1$$

$$\frac{1}{\sqrt{y}} = 2$$

$$1 = 2\sqrt{y}$$

$$\left(\frac{1}{2}\right)^2 = (\sqrt{y})^2$$

$$\frac{1}{4} = y$$

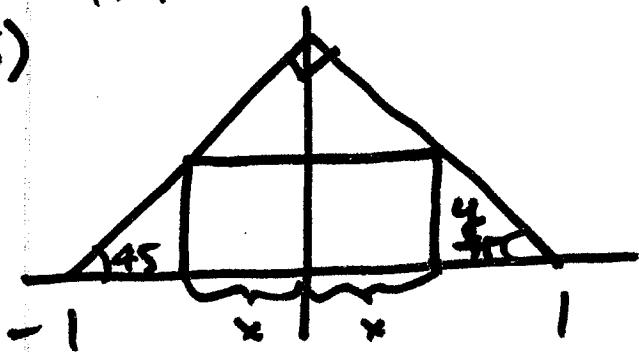


$$-1 + \frac{1}{2}(\sqrt{\frac{1}{4}})^{-1/2}$$
$$-1 + \frac{1}{2}$$

max $\frac{1}{4}, 19\frac{3}{4}$ min 0, 20

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5)

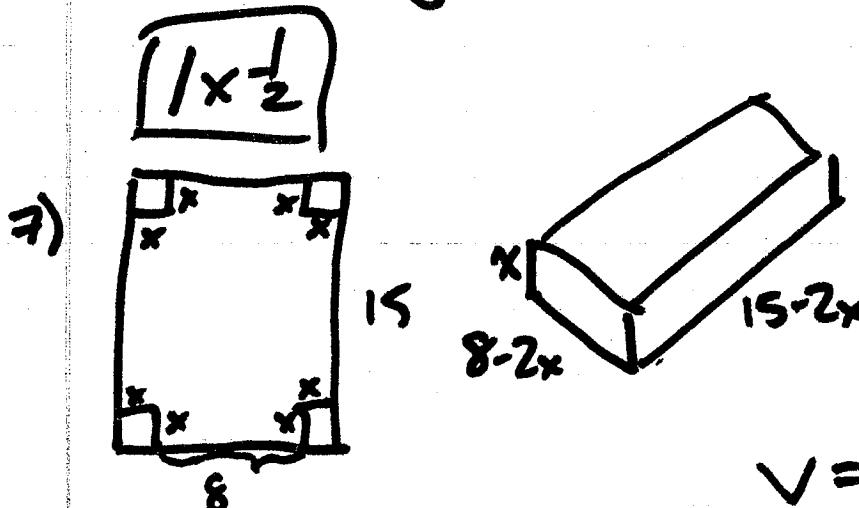


(c) FDT

INCR	DEC
+	-
$\frac{1}{4}$	$\frac{3}{4}$
$\frac{1}{2}$	

~~A~~

$$y = \left(-\frac{1}{2}\right) = \frac{1}{2}$$



$$V = x(120 - 16x - 30x + 4x^2)$$

$$V = 120x - 46x^2 + 4x^3$$

INCR	DEC	INCR
+	-	+
1		7
1	5	6
0		

$$V' = 120 - 92x + 12x^2 = 0$$

$$V' = 4(30 - 23x + 3x^2) = 0$$

$$(5-x)(-3x) = 0$$

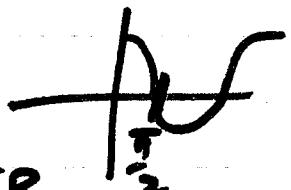
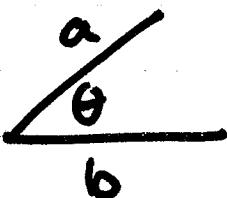
$$(3x-5)(x-6) = 0$$

$$x = \frac{5}{3} \quad x = 6$$

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15) $A = \frac{1}{2}ab \sin \theta$

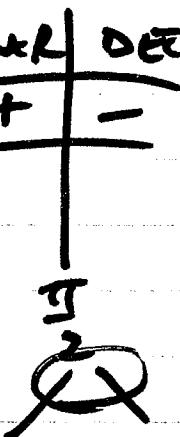
$$A' = \frac{1}{2}ab \cos \theta = 0$$



$$\cos \theta = 0$$

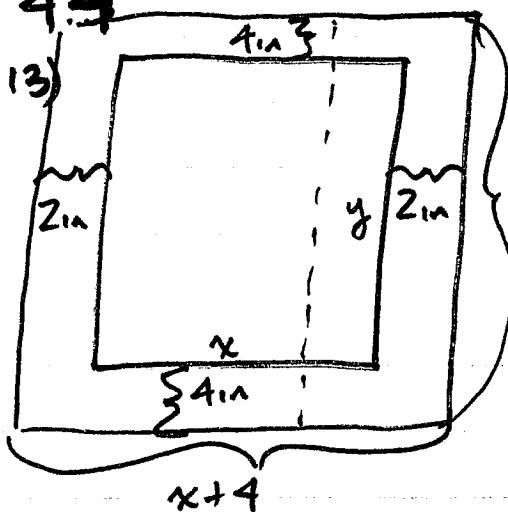
FDT INER DEER

$$\theta = \frac{\pi}{2}$$



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(3)



$$\text{Primary: } A = (x+4)(y+8)$$

$$A = (50y^{-1} + 4)(y + 8)$$

$$A' = -50y^{-2}(y+8) + (50y^{-1} + 4)$$

$$-50y^{-1} - 400y^{-2} + 50y^{-1} + 4$$

$$-400y^{-2} + 4 = 0$$

$$400y^{-2} = 4$$

$$y^{-2} = \frac{1}{100}$$

$$y^2 = 100$$

$$y = \pm 10$$

$$y = 10$$

$$\text{Secondary: } A = xy = 50$$

$$x = \frac{50}{y} = 50y^{-1}$$

EDT

DEC R

INCR

$$-400(5)^{-2} + 4$$

$$-400(11)^{-2} + 4$$

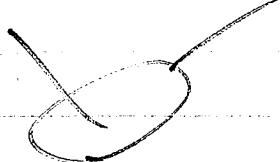
5

11

0

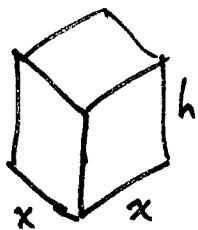
10

10" x 5"



4.4

11)



$$V = x^2 h = 500$$

$$h = \frac{500}{x^2} = 500x^{-2}$$

Primary: $SA = 4xh + x^2$

$$4x(500x^{-2}) + x^2$$

$$2000x^{-1} + x^2 \quad x \neq 0$$

$$SA' = -2000x^{-2} + 2x = 0$$

$$2x = \frac{+2000}{x^2}$$

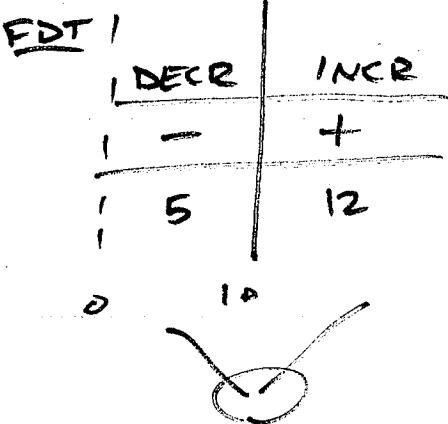
$$x^3 = 1000$$

$$x = 10$$

$$-2000(5)^{-2} + 2(5)$$

$$-2000(12)^{-2} + 2(12)$$

$10 \times 10 \times 5$



15)