

10.1

$$\begin{aligned} 9) \quad x &= -\sqrt{t+1} & y &= \sqrt{3t} \\ x &= -(t+1)^{1/2} & y &= (3t)^{1/2} \end{aligned}$$

$$\frac{dy}{dx} = \frac{\frac{1}{2}(3t)^{-1/2} [3]}{-\frac{1}{2}(t+1)^{-1/2}} = -3 \left( \frac{3t}{t+1} \right)^{1/2} = -9^{1/2} \left( \frac{t+1}{3t} \right)^{1/2}$$
$$= - \left( \frac{3 \cdot 9 (t+1)}{3t} \right)^{1/2}$$

$$= - \left( \frac{3t+3}{t} \right)^{1/2}$$

$$= - \left( 3 + \frac{3}{t} \right)^{1/2}$$

$$\frac{d^2y}{dx^2} = \frac{-\frac{1}{2} \left( 3 + \frac{3}{t} \right)^{-1/2} \left[ -\frac{3}{t^2} \right]}{-\frac{1}{2} (t+1)^{-1/2}}$$

$$= \left( \frac{t+1}{3 + \frac{3}{t}} \right)^{1/2} \left[ \frac{-3}{t^2} \right]$$

$$= - \left( \frac{t+1}{3 + \frac{3}{t}} \right)^{1/2} \left[ \frac{9}{t^4} \right]^{1/2}$$

$$= - \left[ \frac{t+1}{3 + \frac{3}{t}} \cdot \frac{9}{t^4} \right]^{1/2}$$

$$= - \left[ \frac{9t+9}{3t^4+3t^3} \right]^{1/2}$$

$$= - \left[ \frac{9(t+1)}{3t^3(t+1)} \right]^{1/2}$$

$$= - \left[ \frac{3}{t^3} \right]^{1/2}$$

10.1

$$23) x = 2 + \cos t, y = -1 + \sin t$$

$$\frac{dy}{dx} = \frac{-\cos t}{\sin t}$$

$$(a) \text{ HORIZONTAL } -\cos t = 0$$

$$(b) \text{ VERTICAL } \sin t = 0$$

$$25) x = 2 - t, y = t^3 - 4t$$

$$\frac{dy}{dx} = \frac{3t^2 - 4}{-1}$$

$$-3t^2 + 4 = 0$$

$$4 = 3t^2$$

$$\frac{4}{3} = t^2$$

$$\pm \sqrt{\frac{4}{3}} = t$$