

6.3  
 ①7  $\int e^x \sin x dx$

$u = \sin x \quad v = e^x$   
 $du = \cos x dx \quad dv = e^x dx$

$\int e^x \sin x dx = e^x \sin x - \int e^x \cos x dx$   
 $u = \cos x \quad v = e^x$   
 $du = -\sin x dx \quad dv = e^x dx$

$\int e^x \sin x dx = e^x \sin x - (e^x \cos x - \int -e^x \sin x dx)$

$\int e^x \sin x dx = e^x \sin x - e^x \cos x - \int e^x \sin x dx$   
 $+ \int e^x \sin x dx \qquad + \int e^x \sin x dx$

$\frac{2 \int e^x \sin x dx}{2} = \boxed{\frac{e^x \sin x - e^x \cos x}{2} + C}$

②8  $\int_0^\pi x \sin x dx$   
 $u = x \quad v = -\cos x$   
 $du = dx \quad dv = \sin x dx$

$\int_0^\pi -x \cos x + \int_0^\pi \cos x dx$

$\int_0^\pi -x \cos x + \sin x$

$[-\pi \cos \pi + \sin \pi] - [-0 \cdot \cos 0 + \sin 0]$

$\pi$

$\int_0^{2\pi} + \int_0^\pi + \int_\pi^{2\pi}$

$\pi + 3\pi = 4\pi$

$\int_\pi^{2\pi} x \sin x dx$

$\int_\pi^{2\pi} -x \cos x + \sin x$

$[-2\pi \cos 2\pi + \sin 2\pi] - [-\pi \cos \pi + \sin \pi]$

$-2\pi - \pi = -3\pi$

$3\pi$

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 23)  $\int x^3 e^{-2x} dx$

SIGN	u	dv
+	$x^3$	$e^{-2x}$
-	$3x^2$	$-\frac{1}{2}e^{-2x}$
+	$6x$	$\frac{1}{4}e^{-2x}$
-	$6$	$-\frac{1}{8}e^{-2x}$
+	$0$	$\frac{1}{16}e^{-2x}$

$$-\frac{1}{2}x^3 e^{-2x} - \frac{3}{4}x^2 e^{-2x} - \frac{3}{4}x e^{-2x} - \frac{3}{8}e^{-2x} + C$$

11)  $\frac{dy}{dx} = (x+2) \sin x$        $u = x+2$        $v = -\cos x$

$\int dy = \int (x+2) \sin x dx$        $du = dx$        $dv = \sin x dx$

$y = (x+2)(-\cos x) + \sin x + C$   
 $(x+2)(-\cos x) + \int +\cos x dx$

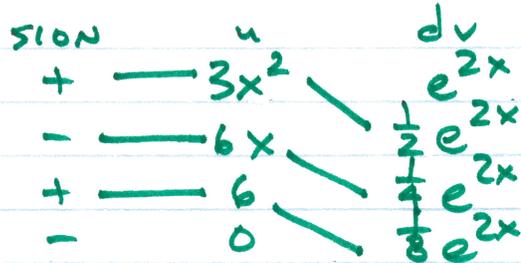
$2 = (0+2)(-\cos 0) + \sin 0 + C$

$2 = -2 + C$

$4 = C$

$$y = (x+2)(-\cos x) + \sin x + 4$$

6.3  
 ⑦  $\int 3x^2 e^{2x} dx$



~~DA~~

$$\frac{3}{2} x^2 e^{2x} + -\frac{3}{2} x e^{2x} + \frac{3}{4} e^{2x} + C$$